THE SENSITIVITY PRINCIPLE IN EPISTEMOLOGY

EDITED BY
KELLY BECKER
and
TIM BLACK



CAMBRIDGE UNIVERSITY PRESS Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paulo, Delhi, Mexico City

Cambridge University Press The Edinburgh Building, Cambridge CB2 8RU, UK

Published in the United States of America by Cambridge University Press, New York

www.cambridge.org Information on this title: www.cambridge.org/9781107004238

© Cambridge University Press 2012

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written

First published 2012

permission of Cambridge University Press.

Printed and Bound in the United Kingdom by the MPG Books Group

A catalogue record for this publication is available from the British Library

Library of Congress Cataloguing in Publication data

The sensitivity principle in epistemology / edited by Kelly Becker and Tim Black.
p. cm.
Includes bibliographical references (p.) and index.
ISBN 978-1-107-00423-8 (hardback)

I. Knowledge, Theory of. I. Becker, Kelly, 1966— II. Black, Tim.
BD161.846 2012
121'.6—dc23

15BN 978-1-107-00423-8 Hardback

2012015434

Cambridge University Press has no responsibility for the persistence or accuracy of URLS for external or third-party internet websites referred to in this publication, and does not guarantee that any content on such websites is, or will remain, accurate or appropriate.

Jonathan Vogel

⋖

Contents

00	7	Þ		6	V	4	w	Ŋ	P	}(7. 1
The enduring trouble with tracking	Truth-tracking and the value of knowledge <i>Jonathan L. Kvanvi</i> g	PART II CRITICISM	Kelby Becker	Methods and how to individuate them	Knowledge, cognitive dispositions and conditionals Lars Bo Gundersen	Sensitivity from others Sanford Goldberg	Sensitivity meets explanation: an improved counterfactual condition on knowledge Peter Murphy and Tim Black	Nozick's defense of closure Peter Baumann	PART I DEFENSES, APPLICATIONS, EXPLICATIONS	The resilience of sensitivity Kelly Becker and Tim Black	List of contributors Preface
122	IOI			18	66	43	28	п		ı	<i>page</i> vii ix

Sensitivity and closure

Sherrilyn Roush

I INTRODUCTION

a brain in a vat - it came at the price of denying closure of knowledge what seemed to be the sensitivity condition's primary selling point. have on that basis knowledge. Many felt this was too much to pay for that q implies p are together sufficient to make the belief in p that you under known implication, that is, denying that knowing q and knowing to know that there is a table in front of you without knowing you are not condition, which requires that were p to be false you wouldn't believe examples. The sensitivity condition, or as Nozick called it the variation due to the failure time and again to construct a theory without counterthis condition for skepticism was elegant and principled – it is possible it, had its own apparent counterexamples. And while the implication of because of loss of faith in the project giving a theory of knowledge at all, by a glamorous implication the condition has for skepticism, and in part in epistemology. This was in part because these resources were upstaged lysis of the concepts of knowledge and evidence, went largely unappreciated concept we now call sensitivity, which Robert Nozick used to give an ana-From the mid 1980s to the early 2000s the wide-ranging resources of the

However, the sensitivity condition need not prevent closure if it is not taken as a necessary condition for knowledge. Drawn to that move's exciting implications about skepticism, no one gave an argument for taking the condition so. Conditions can figure in lots of different ways in the definition of a concept. Sensitivity was already imagined as only one of a set of necessary conditions for knowledge of p, each independent of the others, including belief in p, the truth of p (and in Nozick's theory adherence to p). Why should a definition have exactly this many but no more independent clauses? One might reply that closure should not be a property that is *independent* of the property of knowledge that goes beyond truth and belief; it should follow from that property. The weakness of this

reply is that it is grounds for rejecting other theories, too; few if any of the major theories of knowledge of recent times have that feature.

Alvin Goldman was aware of this fact about his process reliabilist condition on justified belief (and thereby knowledge) from the inception of his theory. That one's true belief in q was formed by a reliable process, and that one's valid deduction of p from q was reliably formed, do not together imply that one's belief in p so formed was formed by a reliable process. This is because reliability of a process is not defined as requiring infallibility, even for deduction, and wherever one sets the threshold, two processes that are just above the threshold can concatenate to one process of error. For this reason Goldman did what any rational person who subscribes to the closure of knowledge or justified belief would; he introduced a recursion clause, allowing that one has a justified belief if either one's belief was formed by a reliable process to a justified belief (Goldman 2008, 340–41).

In internalist views of justification (and potentially, thereby, knowledge) the conditions imposed on the concept(s) are sometimes not defined explicitly enough to deductively imply a verdict one way or the other on closure, or are explicitly defined and do not have an implication one way or the other. (I will deal with Tony Brueckher's example of an internalist view that does imply closure below.) Intuitive arguments, of which there are many, can be taken to provide reasons to add closure as an independent requirement in an internalist view of knowledge, but those intuitions are available to externalists, too. That sensitivity does not imply closure, and taken as a necessary condition easily brings failure of closure, is not a good argument for its being less adequate than other conditions.

In other places (Roush 2005, 2009, 2010a) I have developed, through examination of a number of issues, what I see as the extensive explanatory resources in the concept of sensitivity when it is combined with adherence. Here I will focus on the consequences of the move I made of combining sensitivity (and adherence) with closure via a recursion clause. My imposition of closure on a sensitivity-based view of knowledge has

I think that safety as a necessary condition does achieve closure automatically, without a recursion clause, despite recent arguments to the contrary. When the subject's belief in the conclusion is based on her belief in the premise, the worlds in which the subject believes the conclusion of the implication are a natural subset of the worlds in which she believes the premise. If so then the conclusion belief is as true as the premise belief that implies it. This automatic closure leads to a cheap knowledge problem, though.

seemed to some unexplanatory and to lead to cheap knowledge. I will argue that as it stands the view is no less explanatory, and leads to no more cheap knowledge, than other views. However, my main objective here is to explain why these issues depend very much on the formulation of the closure clause and to present a new formulation. The new view does not have problems with explanation or cheap knowledge, and I will use it to explain how the problem of closure is entirely provoked and resolved by attention to the growth of potential error.

My theory of knowledge is a refiguring of Nozick's theory that uses probability rather than counterfactuals, and in which the sensitivity condition is neither a necessary nor a sufficient condition. Schematically, it is sufficient for subject S to know p, a contingent proposition, if p is true, she believes p, and:

- (I) P(-b(p)/-p) > s, where $s \le I$ and
- 2) P(b(p)/p) > t, where $t \le t$.

That is, the probabilities are high that she does not believe p given that p is false and that she does believe p given that it is true. s and t are thresholds determined by the disutility of false positive and false negative errors respectively for the one who is evaluating whether S knows that p, who may or may not be S herself. "<" rather than "<" accommodates the possibility of an evaluator who has infallibilist utilities. For anyone living outside bizarro world, s and t will be greater than .5.2

There are several reasons why this formulation of sensitivity in terms of conditional probability is superior to the counterfactual version requiring that if p were false the subject wouldn't believe p. Typically a similarity relation is used to determine which set of possible worlds matters in the evaluation of a counterfactual; we want to know whether the consequent is true in the world(s) where the antecedent is true that are most similar to the actual world. With sensitivity this means we want to know whether the person believes p in the -p world(s) most similar to the actual world. Defining a similarity relation in a principled way so as to match the expectations of an epistemic sensitivity property has been elusive, the best accounts giving a list piecemeal, and even if one achieved a match it would be hard to avoid an air of arbitrariness, since everything is similar to everything else in some respect. However, with a conditional probability

approach there is no restriction on which sets of values for other propositions that are compatible with -p, that is, which possible -p scenarios, are taken into account. All go into the weighted average that determines the value of the conditional probability in (1). Still, these sets of -p-compatible values for other propositions only contribute to the evaluation in proportion to their probability; only the *probable* -p scenarios make a significant difference to the value of the conditional probability.

carve out the set of scenarios that matter; they all do. Yet the impossibilworld we are considering it looks just like a full-sized tree when viewed in the space that is left behind. Moreover, this cosmic ray has properties tiny, cosmic ray hits the tree. It vaporizes the tree and stops to sit there looking at it. Now imagine a possible scenario in which a very special, cally. Imagine you know there is a tree in front of you because you are that similarity is not the gist of what makes a possibility matter epistemidraw a line around a certain set of possibilities just so, but it seems to me having an effect. Not only does this seem less artificial than trying to difference at all to whether one has knowledge. It is only if we are infalmake a smaller difference, but also because of the threshold in condition ity of knowledge does not follow, since not only do less probable scenarios from your distance. that sometimes make it look much larger than it is. In fact, in the possible libilists (with s = r) that no scenario's probability is too low to prevent its (1), -p scenarios whose probability is below r-s, s < r, will not make any We thus eliminate the need for an extra similarity relation to carefully

bumping into, than about whether the possibilities are similar. behavior would be in those possible scenarios we have a good chance of whether we have knowledge we seem to care more about what our belief there is a tree in front of you when you are looking at it. The reason, I cosmic ray that looks like a tree does not undermine your knowledge that has been hauled away. But I think we would also say the possibility of a you to refrain from believing there is a tree there in a world in which it truck and cut it down, dig it up, and haul it away. I think we would expect a beholder of the tree, but also plain physically – than is a world in which is surely much more similar to the actual world – not only in the eyes of ligibly different from the actual world in the matters that go beyond p. It improbable occurrences. In fact the possible world described is only negcosmic ray to be possible. The laws are probabilistic and allow for highly think, is that the world described is too improbable to matter. In judging the tree is not there because landscapers come with big equipment and a The laws of physics would not need to be different, or breached, for this

In what follows I will largely ignore the adherence condition or, when it makes no difference, let it tag along by using "tracking" interchangeably with "sensitivity," but the adherence condition remains part of my theory. It does make an important difference, below, in preservation of sensitivity in multiple-premise closure clauses, and in Roush 2010a.

Sensitivity and closure

only if S believes p, p is true, and either: of that). Thus, schematically, S knows p, a contingent proposition, if and something that one knows implies p (and basing one's belief in p on all by tracking p (fulfilling [1] and [2]), but also by believing p and knowing the new tracking view defined in Roush (2005), one can know p not only Neither of conditions (1) and (2) is necessary for knowledge because on

S tracks p (fulfills 1 and 2)

imply p, and S knows $q_1, ..., q_n$. there are q_1, \ldots, q_n , such that q_1, \ldots, q_n together imply p, S knows that q_1, \ldots, q_n

of those changes. sons I will discuss below. The discussion up to that point is independent since changed the recursion clause in this definition, for important rea-"schematically"), but it gives the idea for current purposes. I have also abilities in (I) and (2) are not determinate for reasons I will discuss below in connection with the generality problem (hence the persistent qualifier This is not yet the definition of knowledge, since the conditional prob-

II KNOWLEDGE OF LOGICAL TRUTH

should be no surprise if the kind of responsiveness we should expect for only circumstance in which this problem arises in the first place - so it their negations to be impossible and their probabilities to be o, the truths - at least they are being treated as radically different if we take sive to the way things are. Necessary truths are different from empirical than this. It expects that when we have knowledge we are being responby conditional probability. However, the idea of sensitivity is broader The problem is hard to fix, and it does not go away in the reformulation counterfactuals with impossible antecedents are prima facie undefined. undefined for logical truths because their negations are impossible, and ledge. The sensitivity condition has the well-known problem of being complete the recursion clause and the (schematic) definition of knowknowledge of logical truths and other necessary truths takes a different Obviously a definition of knowledge of logical implication is needed to

appreciation of its truth. even at the intuitive level. One can believe a proposition without proper true no matter what does not imply that a belief in it is responsive to it, wrong; a belief in it is automatically safe. However, a logical truth's being truth means that you wouldn't, indeed couldn't, easily believe it and be ledge (see Roush 2005, 134-36). For example, the necessity of a logical true, and this has trivialized several otherwise promising theories of know-The truth value of a logical truth is the same no matter what, namely

in the neighborhood. no matter what is not my analysis of responsive to logical truths, but it is tain belief would be present in a large set of possible scenarios. Believing requiring not just a belief but a disposition to believe, the fact that a cermatter what do not imply that you believe it no matter what. The latter is logical truth. The facts that you actually believe p and that p is true no would simply be believing it no matter what, and that is not a bad idea. Consider that this condition is not trivialized by the necessity of the the truth value is the same no matter what? One might think that it What could appreciation or responsiveness to a logical truth be when

ing that $q_{\nu},...,q_{n}$ imply p is fulfillment of the following conditions: to each other. Thus, I say the key extra feature beyond true belief in knowtoward the propositions on either side of that relation must be responsive appreciate a logical truth that is an implication claim your belief states would also fail to know the implication. Implication is a relation, so to p. If, were he to give up belief in p he would retain belief in q, he surely believe p, then we would have to say that he does not know that q implies someone believes q, but were he to form a belief in q he would still not mined by them. For example, if contingent q implies contingent p and itions should comply with those relations even when they are not deteron the relations between our beliefs. Your belief states toward proposimpose relations between propositions, and thereby impose requirements What we need to appreciate about logical truths is the way that they

- $P((-b(q_r) \vee \ldots \vee -b(q_n))/-b(p)) > u \leq r$
- $P(b(p)/(b(q_1) \cdot \ldots \cdot b(q_n))) > v \le 1$

probability you believe p given that you have beliefs in all of q, through ability that you do not have one of the qi beliefs given that you do not evaluator, as above. If you know the implication, then by (3') the probhave a belief in p is high. Similarly, if you know the implication then the where u and v are thresholds that depend on the error tolerances of the

J Can no longer see why I required that none of the q, ..., q, be equivalent to q in my original formulation of this condition, but of course I might have been right there and wrong here.

Tony Brueckner objects to this definition on the grounds that a subject's fulfillment of these conditions merely "attests to the firmness of his belief that the implication holds" (Brueckner, "Roush on knowledge: tracking redux?" this volume, 232; hereafter 'RKTR'). But this is a false description of the conditions, for they are not properties of the subject's belief in the implication at all. In fact the belief in the implication and properties (3') and (4') are logically independent, for a person may behave as if the implication is true, withdrawing and according credence to some of the ps and qs according as his credences in others of them change, without having a belief in the proposition "q, ..., qn imply p," and vice versa. If a belief is a disposition to act – my preferred way of thinking about it – we could say that the subject's patterns of willingness or unwillingness to act on p when he is willing or unwilling to act on q,, ..., qn are distinct from his willingness or unwillingness to act on the claim that q,, ..., qn imply p. For a simple example, imagine someone who does not have the concept of logical implication. "

Brueckner's example of the supermarket tabloid trades on the same confusion. He imagines that I have what he calls a "firm" belief that the implication holds, which I got from a screaming National Enquirer headline, and takes firmness of that belief to be the same as satisfaction of (3') and (4'). But this cannot be so because (3') and (4') are not properties of the implication belief. "Firmness" intuitively suggests that I have a certain stubbornness about the implication claim, but I can have that without acting in accord with the relations among beliefs in q., ..., q_n and p, respectively, that that implication dictates. In fact, getting a stubborn belief in the implication from the headline alone as suggested is a good way of imagining not properly acquiring the appreciation of the relations among beliefs that the implication imposes.

Brueckner says that the reason I do not know the implication claim when I acquire it from the headline is that "I fail to see that q implies p, in that I fail to see the logical connection between q and p" (RKTR, 232–33). This assumes a requirement that the subject appreciate the relation that is claimed between q and p, with appreciation defined as seeing, presumably in the metaphorical sense. My view requires that the subject appreciate that relation, with appreciation defined as having dispositions to manage beliefs in p and q in accord with it. The only difference, then, is in how we understand the needed appreciation. Brueckner claims that there is nothing

"epistemic" about the conditions I require for knowledge of logical implication, so his complaint must be based on the difference between "seeing" and differential dispositions to believe. That is, the objection must assume that counterfactual conditions on belief cannot capture what is epistemic. One is free to make that assumption, of course, but it would make the current dispute unnecessary.

able to give an argument for them, and might not be able to formulate the what I say, though, and there are several advantages to my approach intuitions may underlie Brueckner's dissatisfaction with my view. I mean is hard to believe anyone would leave that out of an account - and these tions requires even access to reasons or understanding of why the logical similar in what it is to know them. Leaving out from the requirements are truths of the same type, and we should expect there to be something "If A and B then A" and the independence of the continuum hypothesis general logical rules of which his beliefs are instances. (Even the woman beings are simple ones known by the man in the street, who would not be known, the majority of logical implications that are known by human by researchers require explicit thought and proof if they are to become First, though the kinds of logical and mathematical truths discovered the subject to be in a position to give an argument - perhaps because it truth is true. My definitions have sometimes been mis-cited as requiring the ability of the subject to prove the claim makes that possible. in the street might not be able to do these things.") Yet truths such as ledge of logical and other necessary truths, because none of these defini-Some may be uncomfortable with my externalist approach to know-

One might object that such externalist conditions as I have proposed cannot be nearly enough to explicate what it is for a mathematician to know a theorem. Such knowledge does require the proof, and the understanding that she acquires in that process. This claim appears correct but there is an ambiguity in the notion of requiring. Acquisition of knowledge requires proof in these sophisticated cases, but I am defining what it is to know, not what is required to attain that status. I do not take the process of coming to a belief as related in a necessary way to its status as knowledge. (Counterfactual conditions in general do not; they are current-time-slice-views, not historical views. The claim that I should have a historical view would require an argument on different grounds.) That process is obviously related in a contingent way to the status – it happens to be a psychological fact that some logical knowledge cannot be acquired

⁴ For this reason I expressed doubt about whether we should even have the belief clause in the definition of knowledge of implication (Roush 2005, 47).

⁵ Even logicians have a hard time giving a non-circular proof of the simplest logical truths.

by us except through explicit work — and this is enough to explain the intuition that it should be a requirement for having the knowledge. The objection is also right that proofs can yield deep understanding, but the state of understanding is different from the state of knowing.

alizations of it have become theorems about the "taxicab numbers," but cubes. Of course he subsequently was able to prove the claim, and genera famous anecdote about Ramanujan, that when G. H. Hardy remarked ability for knowledge is committed to there never being any moment at if all of the great mathematicians eventually, or quickly, were able to give denying too much knowledge. unless we stretch the notion of ability in an ad hoc way we are liable to be est natural number representable in two different ways as a sum of two immediately informed his cabmate that the number 1729 was the smallthat the number on the taxicab they were sharing was uninteresting he which a mathematician knows a theorem without that articulation abilproofs of the necessary truths they discovered, a view that requires that not writing them down was due to the need to conserve paper. But even Srinivasa Ramanujan has apparently been exaggerated - the editors of his quences for classification. The prooflessness of the mathematical wonder would fail to explain their similarity. It would also have awkward conseknowledge, and to split the two categories - ordinary vs. sophisticated of necessary truths would leave the man on the street little if any logical ity, never, ironically, a pure "seeing" moment. The journals aside, there is journals from the years in India say it is clear that he had proofs, and his To take the availability of argument as a requirement on all knowledge

Not all logical truths are implication claims, of course, but the relation of implication can guide us through the rest because of the distinctive fact about a logical truth, that it is implied by every proposition in the language. To know non-implicational logical truth, r, then, I say that what we need to be responsive to in our belief behavior is this special relation r has to all other propositions. One does not have to know that r is implied by every proposition in order to know r – most people do not even have that belief. Rather it must be that there is no proposition such that one fails to appreciate the implication relation it has to r. It must not be that one might believe it and not believe r. That is, the proper way to be responsive to a (non-implicational) logical truth is to have a disposition to believe it come what may among one's beliefs. Schematically, the conditions for this are:

(c') For all $q_1, ..., q_n$, $P((-b(q_1) \lor ... \lor -b(q_n))/ -b(r)) > w \le 1$

(d') For all q_1, \ldots, q_n , $P(b(r))/(b(q_1) \ldots b(q_n)) > x \le r,^6$

for w and x thresholds of error tolerance possessed by the evaluator. (See Roush 2005 for more detail.) If a subject knows r, then in a case where the subject did not believe r he would not believe anything, and when he does believe anything, he also believes r.

This is not a requirement for responsiveness to the fact that r is true no matter what, but responsiveness to the relation r has to every proposition one might believe, and thus to the constraints on belief behavior the logical facts impose. The difference between a "come what may" phrasing and a "come what may among one's beliefs" phrasing, is that the latter does not require you to be someone who would believe r even if you believed nothing else; the former does. The difference is not merely technical. It indicates that what being responsive to logical propositions requires is not principally a relation to how the world is as regards logic, but how whatever that truth is imposes requirements on the relations among one's beliefs. This makes my view compatible with a non-realist view that logical truths are not so in virtue of the way the world is, but in virtue of something like convention, or the rules of language or the contours of human concepts. Whatever logical truths are, they impose constraints on belief of the sort I have described.

The phrase "come what may" and the implicit invocation of Quine's web of belief might prompt one to wonder whether the view can plausibly accommodate the fact, or view, that revision of logic could be justified. If in order to know the Law of Excluded Middle (LEM) one must have a disposition to believe it no matter what else one believes, then does it not follow that one could not count as knowing it if one might seriously consider an argument from L. E. J. Brouwer that this principle must be rejected?

This does not follow, for interesting reasons. The dispositions that are required of one are expressed as conditional probabilities whose values must be above a certain level, w or x. Unless the threshold chosen is 1, knowing LEM allows for a probability of 1-x that you would give up that belief given other beliefs. It is legitimate to demand that the probability of your revising, 1-x, is small if we are to count you as knowing, and there are at least two ways of achieving that. If one were a researcher who dealt with arguments about revision of logic on a regular basis then there is a high probability that one would *consider* changing one's mind, but

Though I have used the same labels, c' and d', as I used in the book, these are much simplified, and therefore not fully correct, versions of those conditions.

we would expect such a person not to be a push-over for arguments for radical views, and that keeps the probability of an actual change down. A person in the street not versed in logic might be someone inclined to naïve enthusiasm when presented with radical views, and so would be a pushover when presented with an alternative logic. But he can know LEM, or instances of it, even so, provided he is unlikely to come across or understand accounts of radical logics. As one becomes more and more disposed to changing one's mind about LEM, perhaps due to increasing exposure to alternatives, one's knowledge of it slips away too, on this view, even when one's belief does not change. But this does not seem to conflict with intuitions, because it is a process in which the robustness of one's commitment erodes.

A less realist view of logic, where logical truths are rather viewed roughly on the model of conventions, would bring an additional feature here. On such a view, if you are considering changing your belief in LEM, you are considering changing your language, for changing your logic at least implies this even if it is not identical to it. However, those circumstances of not believing LEM do not violate the conditions on knowing LEM. They would be scenarios in which you don't believe LEM but you don't have other beliefs either in the sense that concerns the conditional probability conditions on your current belief in LEM; what a belief is in that sense is conditioned by your current language. So c' is fulfilled. And in all of the possible beliefs as defined for your current language, including logic, you do have the belief in LEM, so d' is fulfilled. This is another place where the difference between belief come what may and belief come what may among your beliefs shows itself.

Knowledge of necessary truths is fallible – you always might have made a mistake – but it has been difficult to incorporate fallibility in other theories of this kind of knowledge (Roush 2005, 134–36) because the proposition does not have the potential to be false. The view here avoids this problem because the responsiveness one must have is not to the difference between the truth and the impossible falsity of the logically true proposition, but to the relations each of these truths has to other propositions and to the relations they impose on groups of other propositions. The required dispositions are dispositions among your belief only – the question is not what one would do if the logically true proposition were false, but what one would do with one belief given one's belief or lack of belief in another. Most of us will take the parameters w and x to be less than 1 in the conditions above – when we take them as 1 we are infallibilists and the challenge of creating a fallibilist theory does not arise – which means

that the disposition that makes you count as appreciative or responsive need not guarantee that you avoid error in all possible circumstances.

III CLOSURE AND THE GROWTH OF ERROR

Achieving closure via a recursion clause, such as the one above, where the requirements for knowledge of the implication are not infallibilist but have thresholds, has a problem with the growth of error that I did not deal with in my book. Suppose that I track q to degrees s and t and am responsive to degrees u and v to the fact that q implies q'. Let s, t, u, and v each be less than I. It follows from the definition that I know q', although, because the thresholds are below I, my potential error in my belief in q' is higher than the potential error I have in my belief in q. The growth over one step may not be large enough for worry. (We will calculate actual values below.) However, now that I know q' I can do the same thing for any q'' that I know q' implies, and this sequence can be continued indefinitely. It does not need to be carried on very far for me to be counted as knowing things for which my sensitivity is only 50 percent. The same is

What causes the runaway multiplication of potential error is not the allowance of knowledge by known implication but the recursion. However, we can reformulate the relevant clause of the view (see above, 246) without the recursion by changing one word:

S tracks p (fulfills (1) and (2))

or C

there are $q_1, ..., q_n$, such that $q_1, ..., q_n$ together imply p, S knows that $q_1, ..., q_n$ imply p, and S tracks $q_1, ..., q_n$.

The difference occurs in changing the second "knows" to "tracks" in the second clause? It is now not enough to know that p follows from something that you know follows from something that you know ... follows from something that you track. You must instead be no more than one implicational step away from a proposition that you track if you are to count as knowing. This avoids the problem of counting a belief with any old degree of potential error knowledge, because it turns out that any

A similar change is made for knowledge of necessary truths known by known implication from knowledge of other necessary truths. The beliefs in the premises of such an argument would have to fulfill the "sensitivity" requirements for knowledge of non-implicational necessary truths, c' and d' above.

implies a degree of preservation of sensitivity. a tracking belief puts strict limits on the growth of potential error, and designation of the number of allowed steps of known implication from

necessary condition: the belief in p is based on the belief in q only if giving her knowledge of p. I define the basing relation using the following it. In that case there is no good reason to think that her knowledge of q is belief whose knowledge status closure says is supposed to give her a right to clause because otherwise her belief in p is only accidentally related to the in p is based on her belief in q.8 This is a standard assumption in any closure results requires explicit definition of an assumption that the subject's belief Calculating error over known implications in the way that will yield such

P(-b(p)/-b(q)) is high,

q. Fully generally, that is, only if you are unlikely to believe p given that you do not believe

$$(5) \ P(-b(p)/\ (-b(q_1) \lor -b(q_2) \lor \dots \lor -b(q_n))) > z \le r.$$

 q_n would be solely responsible for your belief in p. If this conditional probability were as high as 1 then your beliefs in q_p ...,

ledge of $q_1, ..., q_n$, because the question is whether the latter is sufficient. the only thing you have that might get you knowledge of p is your knowthe closure requirements. In the closure question we are assuming that beliefs that imply p. Rather, this is a claim of basing needed to formulate from also believing or being disposed to believe p on the basis of other q_1, \dots, q_n imply p. Knowing that q_1, \dots, q_n imply p does not prevent you Note that this basing claim is not part of what is required to know that

and only if
(I) P(-(2), (3'), and (4'), S's true belief in p, a contingent proposition, is knowledge if To summarize the whole view, again schematically with regard to conditions (1),

and P(-b(p)/-p) > s, where $s \le I$, (sensitivity to p)

(2) P(b(p)/p) > t, where $t \le I$,

(adherence to p)

there are q_1, \ldots, q_n such that q_1, \ldots, q_n together imply p, S believes that they do, and for every $q \in \{q_1, \ldots, q_n\}$ S fulfills r and r, that is, P(-b(q)/-q) > s, (sensitivity to every premise)

P(b(q)/q) > t, (adherence to every premise)

S fulfills ς for $q_p \dots, q_n$, that is, (ς) $P(-b(p)/(-b(q_1) \vee -b(q_2) \vee \dots \vee -b(q_n))) > z \le r$ (basing b(p) on $b(q_1), \dots, b(q_n)$) S fulfills 3' and 4' for $q_p, ..., q_n$, that is, (3') $P((-b(q_1) \vee ... \vee -b(q_n))/ -b(p)) > u \le t$, or the number of steps of known basing implication is m > 1. (4') $P(b(p)/(b(q_p) \dots b(q_n))) > v \le I$ (implication adherence) (implication sensitivity)

also depend on the error tolerances of the evaluator in a way that we will of known implication also affect the growth of potential error, so m and n For reasons I discuss below, the number of premises and number of steps

First using a single premise q for simplicity, by total probability, the q_1, \ldots, q_n , and the basing of my belief in p on my beliefs in q_1, \ldots, q_n . this is given by the fact that q., ..., qn together imply p, my sensitivity to I do not believe p given that p is false? Information sufficient to determine can we say about the sensitivity of my belief in p? What is the probability If I fulfill all of the clauses beyond "or" in the definition just given, what

$$P(-b(p)/-p) = P(-b(q)/-p)P(-b(p)/-b(q).-p) + P(b(q)/-p)P(-b(p)/b(q).-p).$$

By the fact that -p implies -q, the right-hand side is greater than or equal

$$P(-b(q)/-q)P(-b(p)/-b(q).-q) + P(b(q)/-q)P(-b(p)/b(q).-q).$$

The terms here involve sensitivity to q, basing, and implication adher-

$$(>s)(>z) + (< (I-s))(< (I-v)).$$

Taking all thresholds as .95, this becomes:

$$(>.95)(>.95) + (<.05)(<.05) > .90.$$

from q is diminished from s only by the level of deviation from perfect to q is s, then one's level of sensitivity to some p that one knows follows term in which v occurs is composed of maxima. If one's level of sensitivity tion it has no impact on our question of a minimum because the second s.z. Although level of adherence to the implication, v, occurs in the equa-In general, for one-step, one-premise known implications, P(-b(p)/-p) > 0

g It is such an obvious assumption that I actually left it out in my definition in the book. It was not clear to me then how crucial it is to the calculation of growth of potential error.

basing. If your belief in q is truly the only basis for your belief in p, then no potential error is introduced at all; sensitivity is fully preserved over the known implication. In general, for m-step, one-premise known implications, the preserved sensitivity level, P(-b(p)/-p), is $s \cdot z^m$. Thus, for two steps and all thresholds set at .95, P(-b(p)/-p) is .86, for three steps .81.

Multiple-premise closure brings further error considerations. Each premise known fallibly contributes potential error, so the potential error in the resulting belief in p is greater than it would have been with fewer premises. The question is how much greater. Taking the next case, two-premise implication, we want to know the minimum level of sensitivity one will have to p if one is counted as knowing it by tracking each of q and q, knowing that they together imply p, and basing one's belief in p on them. This can be calculated as follows. Because –p implies –q, which implies –q, the latter, call it A, becomes the condition in all of the conditional probabilities:

$$\begin{array}{l} P(-b(p)/-p) = P((-b(q_i),-b(p),-b(q_i))/A) + P((-b(q_i),-b(p),b(q_i))/A) + \\ P((b(q_i),-b(p),-b(q_i))/A) + P((b(q_i),-b(p),b(q_i))/A). \end{array}$$

The last term is 0 since $P(b(q_i).b(q_i)/(-b(q_i) \vee -b(q_i)))$ is 0. Rewriting each remaining summand,

$$\begin{array}{l} P(-b(p)/-p) = P(-b(p)/(-b(q_i),-b(q_i)))P(-b(q_i),-b(q_i)/A) + \\ P(-b(p)/-b(q_i),b(q_i))P(-b(q_i),b(q_i)/A) + P(-b(p)/b(q_i),-b(q_i)) \\ P(b(q_i),-b(q_i)/A). \end{array}$$

For the moment I will assume that when $-q_1 \lor -q_2$ is the case it is equally likely to be $(-q_1, -q_2)$, $(-q_1, q_2)$, or $(q_1, -q_2)$. The first term is determined by basing and sensitivity to each of q_1 and q_2 and equals:

$$z \cdot s^2/3 = (.95)(.95)(.95)/3 = .29.9$$

The second term is determined by basing, sensitivity to q_{ν} , and adherence to q_{ν} , and equals:

$$z \cdot s \cdot t/3 = (.95)(.95)(.95)/3 = .29.$$

The third term is symmetric to this one and also equals .29. Thus we have that the sensitivity to p that results from knowing it in the way imagined is at least .87. That amounts to 3 percent less fidelity than with one-premise (one-step) implication.

In general, for one-step, two-premise closure, for the conclusion-belief in p,

 $P(-b(p)/-p) = a \cdot z \cdot s^2 + b \cdot z \cdot s \cdot t + c \cdot z \cdot t \cdot s$

What will be a problem for some is the fact that getting lower bounds on sensitivity of the conclusion-belief in the multiple-premise implication case depends crucially on t, the subject's adherence to q, and to q, as it did not in the one-premise case. The renaissance of interest in the sensitivity condition has not been accompanied by enthusiasm for Nozick's adherence condition (except in my case), but it makes a difference in minimizing the growth of error. If one endorsed sensitivity but not adherence, then one would not have general error-control with more than one-premise closure.

IV EXPLANATION OF CLOSURE

Brueckner objects to the recursion clause that I used in the book to impose closure, that it does not explain *why* knowledge would be preserved under known implication. It just stipulates that it is. However, judging by the standard Brueckner sets with the examples of views he thinks do bring with them an explanation of closure, I have to disagree. He has us consider an evidentialist view:

I have good evidence e for q, and I correctly deduce p from q. On what basis do I then know p? An evidentialist can answer that if one has adequate justifying evidence E for ϕ , and ϕ implies ψ , then E is also adequate justifying evidence for ψ .

To simplify the presentation I have made use of the fact that $P(-b(q_i), -b(q_j)/A) = P(-b(q_i), -b(q_j)/-q_i, -q_j)P(-q_i, -q_j/A) = P(-b(q_i), -b(q_j)/-q_i, -q_j)/3)$ and similarly for the other terms. Note that we are given in the assumptions only that we track one q_n at a time, so we have two sensitivity contributions in the term just cited.

 $^{^{\}circ}$ Precisely, the sensitivity is $zs^{3}/7 + 3zsz^{2}/7 + 3zs^{2}z/7$.

This explains how it is that I can know p on the basis of my deduction of p from q: my evidence e for q puts me in a position to know the implied p. (RKTR, 233) If E is evidence for φ , and φ implies ψ , then E is also evidence for ψ . Why should we think this? What is the understanding of evidence that would make it true? The question is not trivial since the definition of evidential support as probabilistic relevance makes it false. The claim is called the special consequence condition, and it is arguably false even on an intuitive notion of evidential support, as illustrated by examples of φ that are conjunctions with independent conjuncts." Even if there is a notion of evidence that makes this claim true, though, it is not obviously so. Citation of a claim very much in need of defense and explanation is hardly an explanation.

should, when the level of reliability was degraded?¹² able processes to preserve knowledge, as Brueckner seems to think we have taken the analogous concatenation of reliable and conditionally reliness of the concatenation will be somewhat degraded? Why should we should take as making a belief knowledge when the level of responsive-Why should two concatenated responsiveness relations yield a relation we to truths in the way that the nature of the truth in question calls for. sensitivity as defined for empirical truths. They are both responsiveness reliability of the process but is conceptually analogous, responsiveness to structure. Just as conditional reliability of a process is not the same as of a reliable process figures in the recursion clause. Although deduction logical implication is not the same as but is conceptually analogous to Brueckner is his implied denial that my view has the same explanatory remains predicated upon the concept of reliability. Where I disagree with cess, so even with the addition of the recursion clause justified belief does not preserve reliability level it is itself a (conditionally) reliable proof closure. Probably the reason Brueckner thinks this is that the notion I agree with Brueckner that Goldman's reliabilist view is explanatory

Thus, my original view had no more problem explaining closure than other views have. It had no more of a problem of endorsing cheap knowledge, either. It counted me as knowing I am not a brain in a vat provided

only that I tracked my hand and knew that this implied I was not envatted. But the principle Brueckner gives us that ensures evidentialist justified belief is closed has the same problem: it implies that having evidence that one has a hand combined with valid deduction of unenvattedness from the evidence gives one evidence that one is not envatted, because according to the principle, the evidence that you have a hand *is* evidence for what follows from your handedness. It does not seem that any of us has evidence that he is unenvatted.¹³

All that said, my view, like the others, did have problems in these areas. The claim I want to defend now is that the new closure clause resolves both of them in one stroke. My original closure clause (and Goldman's) suffered from the uncontrolled error problem, and this is the source, I think, of the sense that closure has been imposed but not explained. But an uncontrolled error problem is also the source of puzzlement about how knowledge itself could be closed. Why else do we pause at the idea that we know it is not a cleverly disguised mule merely by knowing that it is a zebra, except that what gives us apparent knowledge that it is a zebra does nothing to protect us against the error entailed by the presence of a cleverly disguised mule? Similarly with cheap knowledge; why else would we be surprised that we could know we are not envatted by knowing that we have a hand than that what makes us count as knowing the latter does nothing to protect against the error that envattedness would represent?

Because my new template for closure clauses addresses the error problem, it also relieves us of the other two problems in a novel way. Clauses of the new sort will make a theory closed in one sense, but not in another. Starting with the latter, the change from "knows" to "is sensitive to" means that the following standard formulation of closure is not fulfilled:

If S knows q, knows that q implies p, and believes p on the basis of these things, then S knows p.

If we accept one-step closure, though, with thresholds matching our errortolerances for knowledge, the following weaker kind of claim is true:

If S is sensitive to q, knows that q implies p, and believes p on the basis of these things, then S knows p.

[&]quot;An example from Elliott Sober (http://philosophy.wisc.edu/sober/Special%2oConsequence%2o Condition%2006%2oConfirmation%2ohandout.pdf): the hypothesis that an overturned card is the jack of hearts entails that the card will be a jack, but if you learn that the card is red that does not provide support to the claim that it is a jack.

¹⁶ I take the safety condition to be explanatory for the same reason, that deduction is a safe process. But I think that safety achieves closure without a closure clause. This makes closure natural and adds further explanatory force. However, it comes at a price since the view thereby counts as knowledge cases with vast potential error, e.g., a belief that one is not a brain in a vat. The closure is achieved automatically because of a complete disregard for false positive error.

Safety's automatic closure also yields a cheap knowledge problem since if my hand-belief is safe then it follows automatically that my belief I am not envarted is safe. (And this latter conforms with intuitions under the assumption of the safety of the premise.) We balk at the idea that that is enough for knowledge, though, illustrating that safety, as technically defined, is not enough for knowledge.

The stronger claim can be achieved by a recursion clause only on pain of the snowballing error problem. However, when intuitive arguments are given in favor of closure, the supporting examples involve no more than one known implication and are not direct evidence of a recursion. This and the fact that the growth of potential error is controlled in the new view makes this new kind of closure clause seem to me to capture well what is intuitively right about the claim that knowledge is closed. It is a bonus that we now also know how to define clauses allowing m steps and multiple premises in a way that maintains a specified maximum of potential error and minimum of sensitivity in the conclusion belief.

The consequences of this shift in attention are distinctive. I have not given a closed theory of knowledge with sensitivity as a necessary condition. However, it follows from what we have just seen that for every level of sensitivity, y, there is a disjunctive theory with a sensitivity condition using a threshold greater than y and a one-step, single-premise closure clause that will ensure that no belief whose sensitivity is below y will count as knowledge. The condition that tells you how to find such a theory is: s·z > y. There are many such theories, with varying values for s and z, and there are also all of the theories for multiple-step, single-premise known implications where s·z^m > y, and similarly for multiple-premise known implications where z·sⁿ > y. For every theory fulfilling my definition with sensitivity as a necessary condition, and so with knowledge not closed, there is a theory (following my definition) that is at least as strong in the sensitivity requirement and according to which knowledge is closed in the weaker sense stated above.

One can make knowledge as expensive as one likes with regard to sensitivity, and still maintain a kind of closure. But have we trivialized what it is for a theory to take knowledge as closed? The point of adding a closure cause to a theory by brute force was to make the knowledge concept more permissive. But if a definition requires a belief to have sensitivity > s in order to count as knowledge, then we add nothing to the extension of the concept if we disjoin this condition with one describing a belief that the subject inferred from a belief that has sensitivity > r = s/z. That belief by inference counts as knowledge because we chose the threshold r so that the resulting inferred belief would achieve sensitivity > s! The ability to define and calculate error control over steps of inference does not need to change the extension of the concept of knowledge; what the bounds on the growth or error allow us to do is identify a multiplicity of types of inferences - permutations of values of s, t, m, n, and z - that will yield knowledge of a given sensitivity.

cation from a sensitive belief while knowing nothing more than that error closure, namely, that we can accept a case as knowledge by known implidefined) board of our choice. They give us what is essential to the idea of we can accept knowledge by inference not piecemeal but across the (errorbe closure clauses? I say they are because they explain to us how and why If that problem disappears, though, one might wonder, could these really ant surprise of a forced choice between cheap knowledge and skepticism. shown how to define closure clauses so that they won't yield the unpleasthe principled way to draw lines is in terms of potential error, and I have of the latter. Both sorts of examples are logical implications, after all. I say principled way of identifying the former without stepping into the abyss addressing the problem that I think makes the yes-no question persist. the form of a yes-no question - closure or not? - that is a side-effect of won't have any surprises about the sensitivity of the conclusion-belief. thresholds were met on the initial belief and the basing relation. And we knowledge and where it disastrously fails, and we are at a loss to see a Examples can be found where known implication does seem to preserve This analysis does undercut the interest of the closure problem in

Y LOGICAL IMPLICATION: TOUGH, NOT CHEAF

Brueckner's complaint about the bruteness of my imposition of closure occurs within an objection to the consequences of my view for brain-in-a-vat skepticism. The premise-belief of the skeptical argument — I have a hand, say — is sensitive, but the conclusion-belief — I am not a brain in a vat — is not. Why should we think that the latter is knowledge? With the results I just derived about error the skeptical case becomes even more puzzling. How can it be that sensitivity is largely preserved in one-step deductive inferences, as I just argued a priori, when in the skeptical case we get in one step from a premise and an inference with as much sensitivity as you like to a conclusion with maximum potential error?

In fact neither my original recursive closure clause nor my new closure template implies that it is possible to know you are not a brain in a vat just in virtue of knowing you have a hand and knowing that unenvattedness follows. This is because in this skeptical case the familiar implication claim is false; false claims cannot be known so the premises of the closure clauses are not fulfilled.

That I have a hand does not imply that I am not a brain in a vat because I could be a brain in a vat with a hand. One might think this is cute — smart undergraduates say it regularly — but merely a verbal trick.

Of course one might still be a brain in a vat with a hand. The point was that one could not be a handless brain in a vat if one has a hand. However, though that does give us an implication it is not one that holds any surprises that a skeptic could exploit. If you know that you have a hand then you know that you are not a handless anything. I claim that any attempt to repair the lack of implication between these two claims is doomed to fail, and have argued this elsewhere (Roush 2010b). Strengthening the antecedent sufficiently to get the implication means that supposing we know it is supposing we know a lot, plenty enough, on intuitive grounds independent of commitments about closure, to know we are not brains in vats. Weakening the conclusion to where it is implied by having a hand similarly gives us no surprise that a skeptic could take advantage of; knowing what the deduction lets you know in that case is not knowing much. The lack of implication in the skeptical case means that my closure clauses do not imply something that they cannot explain.

Logical implication is mercifully unforgiving, something I noticed in the context of skepticism only after writing the book, but had noticed in the book in the context of lottery propositions. That I will not have large sums of money tomorrow – something people think I know – doesn't imply that I won't win the lottery today. I could win and promptly be robbed, in whatever sense is needed to relieve me of money in an electronic age – perhaps the girl with the dragon tattoo hacks into the lottery company's account. The usual response to this point is a casual remark to the effect that an example that did involve implication could be constructed. However, I argued in the book that this is not so, because of the same kind of trade-off for the lottery case, so I will leave it at that.

Bruecknet wrongly thinks there is an asymmetry, though, between my treatment of literal lotteries and the kind of lotteries discussed by Jonathan Vogel (1990). Surely I know that my car is parked in the F-lot — I parked it — but I do not know it wasn't stolen while I was sitting in my office for these many hours, even though the latter follows. The same point is true with this case as with the lottery: the implication does not hold because, for example, my car could still be in the F-lot while having been stolen, re-stolen, and returned to its original place. I don't have to know my car wasn't stolen in order to know it is parked in the F-lot, because the former does not follow from the latter. Similarly, I don't have to know I won't win the lottery in order to know what I do seem to know, that I won't have large sums of money tomorrow, because that I won't have lots of money tomorrow doesn't imply that I won't win the lottery today. I do

know that my car was *probably* not stolen, though, because this I track. The probable scenarios in which it was probably stolen – such as that the theft rate is very high in the F-lot – are also scenarios where I wouldn't believe it was probably not stolen. I claim the analogous thing in the literal lottery. Intuitively, I do know that I will probably not win the lottery, and the sensitivity condition explains this: if I were not probably going to lose I would not believe I was probably going to lose.

Logical implication is tough. It must be that there is no possible circumstance in which the premises are true and the conclusion false. It is distinct from any induction with however so many instances one might induce from, and, as I made clear in the book, I do not allow a closure clause for induction. Brueckner finds the implications of this for the bootstrapping argument strange. I find his objections unpersuasive.

The familiar bootstrapping argument (Vogel 2000) has me sitting in the driver's seat of my car with no reason to trust my gas gauge. I engage in the follow procedure: I look at my gauge and form the belief that it has a certain reading, say "F", and on the basis of what it says I form the belief that my gas tank has the amount of gas the reading indicated. I conjoin those two beliefs. I do this, and nothing else, n times, and now I have a list of beliefs in conjunctions. As Brueckner writes it:

- I. My gauge says 'F' and the tank is full.
- .. My gauge says '1/2F' and the tank is half-full.
- 3. My gauge says 'F' and the tank is full.
- 4. My gauge says '1/4F' and the tank is one-quarter-full.

n. My gauge says '34F' and the tank is three-quarters-full.

From I I infer that my gauge was accurate on occasion I, since a match between what it says and what is the case is what accuracy amounts to. I do this for each of I through n and now have many beliefs of the form "My gauge was accurate on occasion m," for many distinct m. I infer from all of these instances that:

: My gauge is reliable.

Clearly this inference does not yield knowledge of its conclusion. I claim that I do not know C in this way because I do not track it: if my gauge were not reliable I would still believe it is because of the silly procedure I am using. If the gauge reading often did not match the gas level in the

tank, that is, if it were not reliable, I would still believe it is reliable. A lack of sensitivity is what is wrong with the fact that I am not checking the accuracy of the gauge except by consulting the gauge.

Brueckner finds this strange, apparently because I am sensitive to the conjuncts in the premises¹⁴ and we can make n as large as we like; what then is the reason for distinguishing this inference over many instances from a bona fide deduction and applying the closure clause? He compares the argument here that I say does not yield knowledge of the conclusion to an argument of a neighbor that could be written down with the same sentences but in which he gets his beliefs by checking the actual level of gas in the tank when he comes to believe the second conjunct in each premise. Brueckner finds it strange that there are two arguments with exactly the same conclusion-beliefs and premise-beliefs and that it follows from my view that my argument does not yield knowledge whereas my neighbor's does yield knowledge. I would have thought that is exactly the consequence one would want a view to have about these cases, since the neighbor does know and I do not. It is evident from the example itself, and not some quirk in my view, that the reason for this difference will not be found in the sentences written on the paper.

Intuitively, the reason the neighbor knows that the gauge is reliable is that he has checked the level of the tank through another means than the gauge. This feature of his procedure also has the implication that he is *sensitive* to the reliability of the gauge. In case the gauge is not reliable chances are good – and better the higher the n – that mismatches will show up between what the gauge says and what the neighbor comes to believe is the level of the tank, because he is investigating the latter by an additional method. The neighbor knows because he tracks. I don't know because I don't track.

It is very neat when the consequences of a theory match intuitions, but am I arbitrarily distinguishing an induction of n instances – n very, very large – from a deduction? What is the big difference between deduction and a very strong induction? I think a closure clause for induction must be rejected because of the same issues about growth of error that I dealt with above in reformulating the closure clause for deduction. There we were able to derive strict upper bounds on the amount of error that taking a merely known-to-be-implied belief as knowledge would give us. With induction we will not be able to derive a reasonable upper bound on error.

One might think that the only difference between the deductive and inductive cases is the strength of the support of the conclusion by the

premises. Every term in the evaluation above depended on the fact that q implies p in order to change the condition -p in P(-b(p)/-p) to the condition -q, so that the sensitivity to q could do its work. But we would expect of a good induction that its evidence, q, made its conclusion, p, probable, say P(p/q) > .95, so would we not just change a 1 for a .95 in every term in that move from -p to -q? Changing 1 to .95 even in four terms would not make a devastating difference. However, this is not the only change that would have to happen. The problem is that an induction must use many pieces of evidence if it is to establish a strong support relation, and although we saw that having two premises rather than one reduced the sensitivity we got for p only by 3–4 percent with the deductive closure clause, thirty pieces of data would make for thirty premises and bring us to no sensitivity at all. And thirty is a small data set.

But suppose for a moment that our thresholds were high enough that a thirty-premise implication would not lose more than 5 percent sensitivity, and suppose that it was possible for human beings to be squeaky clean enough to fulfill those thresholds with the right kind of effort. An inductive closure clause would still not count the inference to the reliability of the gas gauge as giving knowledge. A key part of the reason that sensitivity transmits to a degree over known deductive implication was the sensitivity the subject is required to have to each of the premises. The inductive closure clause would have this requirement, too. However, the premises of the inference to the reliability of the gauge are claims of accuracy of the gauge, and the subject is not sensitive to such claims. If the gauge were not accurate on a given occasion, that is, if the reading the subject saw did not match the actual gas level, the subject would still believe it was accurate, since she is not checking the actual level. This is true for all of the occasions, and so, premises.

An inductive closure clause would be either pointless – because one or two premises rarely give strong support – or disastrous – because a sufficient number of premises, and feasible thresholds, would leave us without any sensitivity to the conclusion proposition. And it wouldn't help to undercut my conclusions about the gas gauge in any case.

There is another apparent problem of cheap knowledge by known implication that my view does not fall prey to. Conjunctions appear problematic because the conjuncts may have properties as different as you like. In a case where if the conjunction were to be false the most similar worlds all have the one false and the other true, and the one that would be false

^{4.} I track the second conjuncts because the gauge is assumed actually to be reliable. The issue is whether I know that it is.

This feature did not come up in my original presentation in the book because the closure clause was recursive.

ment can be imagined against conditional-probability tracking, so it is implied by the conjunction (Roush 2005, 110-12). The same kind of arguif she can know the conjunct she is not sensitive to at all by knowing it is important to see how my views avoid this. the conjuncts. If this is combined with a closure clause, then it looks as counts as sensitive to the conjunction without being sensitive to one of the subject tracks but the other conjunct she does not track, then she

the conjuncts to get fixed and the sensitivity condition for the conjunction is false. In many of those cases the logical properties of conjunctions force conjunct, A, is more likely than the other, B, to be false if the conjunction sibility of fulfilling the sensitivity condition for a conjunction where one out, though I had not anticipated it, that these conditions restrict the posable to pick up on is the difference that -p makes to the world.16 It turns sponding proposition is to be fixed or variable. They are designed to let vary, for example for sensitivity, those matters that are more affected by subclass constrained by conditions that tell us which propositions are to -p than -p is affected by them because what we expect the subject to be tional probabilities ((1) and (2)) must be true in a subclass of that class, a conditions that are responsible for the qualifier "schematically" They give an answer, for every sentence, whether the value for its correhave their probability values fixed in the evaluation (Roush 2005, 76–93). probability functions on the language of evaluation. The familiar conditracking conditions in my theory are quantifications over the class of all that a person is sensitive to many conjunctions of this type, because of the conjunction problem? First, my theory (old or new) does not allow from a belief that is sensitive, so how does my theory manage to avoid that cheap knowledge cannot be had by known implication and basing Obviously, it follows from the results I explained in the previous section above, The

a level as would be needed if one tracked each conjunct and did a multiadherence condition is required for this sensitivity to the conjunction. tion of sensitivity over multiple-premise deduction, no fulfillment of the ple-premise deductive inference to the conjunction. Also, unlike preservato give the conjunction-belief threshold sensitivity, however not at as high each conjunct at a somewhat higher level than the set threshold in order conjunction requires tracking of each conjunct. One has to be sensitive to sitive to generalizations with lots of instances of the same type and to propositions like "It is a black house." But in that case sensitivity to the P(-B/- (A.B)). This is a good thing since it should be possible to be senpossibility of sensitivity to a conjunction in cases where P(-A/ – (A.B)) \approx Fortunately the sieve is not too restrictive, in that it does allow the

explained that knowledge of a proposition one is grossly insensitive to canconjunction one is sensitive to? Obviously, it follows from the results I just so how does my theory manage to avoid the conjunction problem? not be had by known implication and basing from a belief that is sensitive, knowledge of a conjunct one is not sensitive to that can be derived from a to the fixing conditions, then how do I avoid the problem of the cheap one entirely while being committed to the other. But if there are exceptions but only to the probable -p scenarios. It would be arbitrary to rule out the possible scenario in which p is false in order to be counted as knowing p, is very unlikely to be false if the conjunction is false, by the same fallibilism where it is possible to track a conjunction without tracking a conjunct that that says we don't have to be disposed to respond properly to every logically The fixing conditions would seem to be right to allow some exceptions

-b(A.B)) is above threshold z.¹⁸ But she must be sensitive to B to fulfill be based on her belief in the conjunction A.B, it must be that P(-b(B))from the definitions since in order for the subject's belief in, say, B, to ition she is insensitive to, because of that insensitivity. This can be proved requires for closure is not fulfilled for the subject's belief in the propos-Interestingly, it is because the basing condition that my type of clause

¹⁶ The conditions also determine whether methods are fixed; so, methods are not always fixed, but random fabricator's method is fixed at what it is on the occasions when she actually uses her eyes, as I did not notice in the book (Roush 2003, 127-28). not, which I say is a good thing (Roush 2005, 68-71, 112-13). The conditions also imply that the used is independent of the truth value of p. Nozick's case of a father of an accused criminal does one common situation where the conditions imply they are is where whether that method was

The theory (Roush 2005, 76–93) says that if a proposition, A, satisfies the following two conditions, together called "*", then it is fixed in the evaluation of sensitivity:

 $[|]P(-A/-p)-P(-A/p)|\leq |P(-p/A)-P(-p/-A)|,$ $|P(A/-p)-P(A/p)| \le |P(-p/A)-P(-p/-A)|$ and

the conditions for a conjunct, A, being fixed are: where p is the proposition that may or may not be known. Now, if p is a conjunction A.B, then

 $[\]begin{split} & |P(A/-(A.B))-P(A/(A.B))| \le |P(-(A.B)/A)-P(-(A.B)/-A)| \text{ and } \\ & |P(-A/-(A.B))-P(-(A/A.B))| \le |P(-(A.B)/A)-P(-(A.B)/-A)|. \end{split}$

 $P(-A/-(A.B)) \leq P(B)$. Due to the logical relations between conjunctions and their conjuncts both conditions become:

filled, so the theory does not let one know that without tracking it. P(-b(B)/-b(A.B)) = P(-b(B)/-B)P(-B/-b(A.B)). violated, for example when either A or B, or both, have very low probability. However, if either with -(A.B) in the condition, is undefined. There are cases where one or another of these is If both A and B (switching places with A) get fixed in this way then the sensitivity condition, conjunct has very high probability, e.g., "I will not win the lottery tomorrow," then they are ful

tivity. Thus, one cannot cheaply know a conjunct one is insensitive to via the new type of closure clause discussed above. basing, and the intuitively strong counterexamples involve gross insensithis, and she is not. Indeed the less sensitive she is to B, the less she fulfills

VI TAKING STOCK

any level of closure clause we might accept, and are surprisingly reassura difference to how epistemically sound the belief is, I keep track of the will be varying strengths of sensitivity. Since the level of sensitivity makes ing about how quickly (or rather, slowly) error grows. This in turn allows results of these calculations allow us to know the error consequences of tem the behavior of error over known implication can be calculated. The so directly.) Once this is done, then because probability is an axiom systional probability over counterfactuals that these degrees can be expressed expected degrees via variables for thresholds. (It is an advantage of condiskepticism. The closure problem is really an error problem. us to avoid all sorts of cheap knowledge problems, and even brain-in-a-vai Any time one uses a sensitivity condition that is not infallibilist, there

Bibliography

Adams, F., Barker, J., and Figurelli, J. 2011. "Towards Closure on Closure," Synthese DOI: 10.1007/811229-011-9922-8 (Online First).

Adams, F. and Clarke, M. 2005. "Resurrecting the Tracking Theories," Australasian Journal of Philosophy 83:2, 207-21.

Alfano, M. 2009. "Sensitivity Theory and the Individuation of Belief Formation

Linguistics and Philosophy 32:2, 207–44.
Alspector-Kelly, M. 2011. "Why Safety Doesn't Save Closure," Synthese 183:2, Alonso-Ovalle, L. 2009. Methods," *Erkenntnis* 70:2, 271–81. nso-Ovalle, L. 2009. "Counterfactuals, Correlatives, and Disjunction,"

Aquinas, T. 1955. Summa contra Gentiles, trans. Anton Pegis (Garden City, NY: Doubleday & Co.).

Backtracking Conditionals."

Ayer, A. 1956. The Problem of Knowledge (London: Macmillan).

Bach, K. 1985. "A Rationale for Reliabilism," The Monist 68:2, 246–63. Arregui, A. Unpublished manuscript. "Layering Modalities: The Case of

Barke, A. 2002. The Closure of Knowledge in Context (Paderborn: Mentis).

Barker, S. F. 1987. "Conditionals and Skepticism," in S. Luper-Foy, ed. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ: Rowman &

Littlefield), 282-96.

Baumann, P. 2009. "Reliabilism – Modal, Probabilistic or Contextualist," Grazer Philosophische Studien 79:1, 77-89.

Becker, K. 2006. "Is Counterfactual Reliabilism Compatible with Higher-Level Knowledge?" Dialectica 60:1, 79-84.

2007. Epistemology Modalized (New York: Routledge).

2009. "Margins for Error and Sensitivity: What Nozick Might Have Said," Acta Analytica 24:1, 17-31.

Bennett, J. 2003. A Philosophical Guide to Conditionals (Oxford University

Bird, A. 1998. "Dispositions and Antidotes," Philosophical Quarterly 48:191, 2000. "Further Antidotes: A Reply to Gundersen," Philosophical Quarterly

50:199, 229-33.

Black, T. 2002. "A Moorean Response to Brain-in-a-Vat Skepticism," Australasian Journal of Philosophy 80:2, 148-63.

2008. "Defending a Sensitive Neo-Moorean Invariantism," in V. F. Hendricks Macmillan), 8-27. and D. H. Pritchard, eds. New Waves in Epistemology (Basingstoke: Palgrave

Black, T. and Murphy, P. 2007. "In Defense of Sensitivity," Synthese 154:1, 53-71.

Brueckner, A. 1991. "Unfair to Nozick," Analysis 51:1, 61-64.

1994. "The Structure of the Skeptical Argument," Philosophy and Phenomenological Research 54:4, 827-35.

Carrier, L. S. 1971. "An Analysis of Empirical Knowledge," Southern Journal of Philosophy 9:1, 3-11.

Chisholm, R. 1957. Perceiving: A Philosophical Study (Ithaca, NY: Cornell University Press).

1977. Theory of Knowledge, 2nd edn. (Englewood Cliffs, NJ: Prentice-Hall). Choi, S. 2003. "Improving Bird's Antidotes," Australasian Journal of Philosophy

2008. "Dispositional Properties and Counterfactual Conditionals," Mind 117:468, 795–841. 81:4, 573–80.

Church, I. 2010. "Getting 'Lucky' with Gettiet," European Journal of Philosophy DOI: 10.1111/j.1468-0378.2010.00433.x (Online First).

Coffman, E. J. 2007. "Thinking about Luck," Synthese, 158:3, 385–98. Cohen, S. 1988. "How to Be a Fallibilist," Philosophical Perspectives 2, 91–123. 1998. "Two Kinds of Skeptical Argument," Philosophy and Phenomenological Research 58:1, 143-59.

1999. "Contextualism, Skepticism, and the Structure of Reasons," Philosophical

and Phenomenological Research 65:2, 309–29. Comesaña, J. 2005. "Unsafe Knowledge," Synthese 146:3, 393–402. Perspectives 13, 57–89. 202. "Basic Knowledge_and the Problem of Easy Knowledge," Philosophy

Craig, E. 1990. Knowledge and the State of Nature (Oxford University Press). Cross, T. 2010. "Skeptical Success," in T. Gendler and J. Hawthorne, eds. Oxford

David, M. and Warfield, T. A. 2008. "Knowledge-Closure and Scepticism," in Studies in Epistemology, vol. III (Oxford University Press), 35-62.

Q. Smith, ed. Epistemology: New Essays (Oxford University Press), 137–87. Davies, M. 1998. "Externalism, Architecturalism and Epistemic Warrant," in C. Wright, B. Smith, and C. Macdonald, eds. Knowing Our Own Minds (Oxford: Clarendon Press), 321-61.

C. Peacocke, eds. New Essays on the Apriori (Oxford: Clarendon Press), "Externalism and Armchair Knowledge," in P. Boghossian and

DeRose, K. 1995. "Solving the Skeptical Problem," Philosophical Review 104:1, 1–52. Reprinted in K. DeRose and T. Warfield, eds. (1999) Skepticism: A Contemporary Reader (Oxford University Press), 183–219.
1996. "Knowledge, Assertion and Lotteries," Australasian Journal of Philosophy

2000. "How Can We Know that We're Not Brains in Vats?" Southern Journal of Philosophy 38:supplement, 121-48.

Bibliography

Dretske, F. 1970. "Epistemic Operators," Journal of Philosophy 67:24, 1007–23. 1971. "Conclusive Reasons," Australasian Journal of Philosophy 49:1, 1-22. 2010. "Insensitivity Is Back, Baby!" Philosophical Perspectives 24:1, 161-87.

1975. "Review of Armstrong's Belief, Truth and Knowledge," Journal of

Philosophy 72, 793–802.
Feldman, R. 1985. "Reliability and Justification," The Monist 68:2, 159–74.
von Fintel, K. 2001. "Counterfactuals in a Dynamic Context," in M. Kenstowicz,

Frankfurt, H. 1969. "Alternate Possibilities and Moral Responsibility," Journal of ed. Ken Hale: A Life in Language (Cambridge, MA: MIT Press).

Philosophy 66:23, 829–39.
Fumerton, R. 1987, "Nozick's Epistemology," in S. Luper-Foy, ed. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ: Rowman & Littlefield),

Garrett, B. J. 1999. "A Sceptical Tension," Analysis 59:3, 205-6.
Gendler, T. S. and Hawthorne, J. 2005. "The Real Guide to Fake Barns: A Catalogue of Gifts for your Epistemic Enemies," Philosophical Studies

Goldberg, S. 2007. Anti-Individualism: Mind and Language, Knowledge and 124:3, 331–52. Gettier, E. 1963. "Is Justified True Belief Knowledge?" Analysis 23:6, 121–23.

2010. Relying on Others: An Essay in Epistemology (Oxford University Press). Goldman, Alvin. 1967. "A Causal Theory of Knowing," Journal of Philosophy Justification (Cambridge University Press).

1976. "Discrimination and Perceptual Knowledge," Journal of Philosophy 73:20, 64:12, 357-72.

771–91.

1979. "What Is Justified Belief?" in G. Pappas, ed. Justification and Knowledge Publishing), 333-47. M. McGrath, eds. (2008) Epistemology: An Anthology (Oxford: Blackwell (Dordrecht: D. Reidel), 1-23. Reprinted in E. Sosa, J. Kim, J. Fantl, and

1983. "Review of Nozick's Philosophical Explanations," Philosophical Review

Goldman, Alan H. 1987. "Nozick on Knowledge: Finding the Right Connection," 1986. Epistemology and Cognition (Cambridge, MA: Harvard University Press). in S. Luper-Foy, ed. The Possibility of Knowledge. Nozick and His Critics (Totowa, NJ: Rowman & Littlefield), 182–96.

Graham, P. 2000. "Transferring Knowledge," Noûs 34:1, 131–52. Greco, J. 2003a. "Virtue and Luck, Epistemic and Otherwise," Metaphilosophy

34:3, 353–66. 2003b. "Knowledge as Credit for True Belief," in M. DePaul and L. Zagzebski, eds. Intellectual Virtue: Perspectives from Ethics and Epistemology (Oxford University Press), 111–34.

2007. "Worries about Pritchard's Safety," *Synthese* 158:3, 299–302. Unpublished manuscript. "Knowledge, Virtue and Safety."

Greco, J. and Henderson, D. eds. (forthcoming) Epistemic Evaluation: Point and

Purpose in Epistemology (Oxford University Press).
Grobler, A. 2001. "Truth, Knowledge, and Presupposition," Logique et Analyse 44:173-75, 291-305.

Gundersen, L. 2002. "In Defence of the Conditional Account of Dispositions," Synthese 130:3, 389–411.

2003. Dispositional Theories of Knowledge: A Defence of Aetiological Foundationalism (Aldershot: Ashgate).

2004. "Outline of a New Semantics for Counterfactuals," Pacific Philosophical Quarterly 85:1, 1-20.

Erkenntnis 72:3, 353-64. "Tracking, Epistemic Dispositions and the Conditional Analysis,"

Harman, G. 1973. Thought (Princeton University Press).

1986. Change in View: Principles of Reasoning (Cambridge, MA: MIT Press).

Hawthorne, J. 2004. Knowledge and Lotteries (Oxford: Clarendon Press).

Debates in Epistemology (Malden, MA: Blackwell Publishing), 26-41. 2007. "A Priority and Externalism," in S. Goldberg, ed. Internalism and 2005. "The Case for Closure," in M. Steup and E. Sosa, eds. Contemporary Externalism in Semantics and Epistemology (Oxford University Press)

Heil, J. 2003. From an Ontological Point of View (Oxford University Press). Hetherington, S. 1998. "Actually Knowing," Philosophical Quarterly 48:193. 20I-I8.

2002. Good Knowledge, Bad Knowledge: On Two Dogmas of Epistemology (Oxford University Press).

in press. "There Can Be Lucky Knowledge," in M. Steup and J. Turri, eds. Contemporary Debates in Epistemology, 2nd edn. (Oxford: Blackwell

Publishing).
Hiller, A. and Neta, R. 2007. "Safety and Epistemic Luck," Synthese 158:3.

Hilpinen, R. 1988. "Knowledge and Conditionals," Philosophical Perspectives 2, 157-82.

Howard-Snyder, D., Howard-Snyder, F., and Feit, N. (2003). "Infallibilism and

Gettier's Legacy," Philosophy and Phenomenological Research, 66.2, 304–27. Hughes, C. 1996. "Giving the Skeptic Her Due?" Epistemologia 19:2, 309–26. Johnston, M. 1992. "How to Speak of the Colors," Philosophical Studies 68:3.

Kaplan, D. 1989. "Demonstratives," in J. Almog, J. Perry, and H. Wettstein, eds. *Themes from Kaplan* (New York and Oxford: Oxford University Press),

Kelp, C. 2009. "Knowledge and Safety," Journal of Philosophical Research 34

21-31.

2011. "In Defence of Virtue Epistemology," Synthese 179:3, 409-33.

Klein, P. 1971. "A Proposed Definition of Propositional Knowledge," Journal of Philosophy 67:16, 471-82

1981. Certainty: A Refutation of Scepticism (Minneapolis: University of Minnesota

Nozick and His Critics (Totowa, NJ: Rowman & Littlefield), 267-81.

1995. "Skepticism and Closure: Why the Evil Genius Argument Fails," 1987. "On Behalf of the Skeptic," in S. Luper-Foy, ed. The Possibility of Knowledge.

Philosophical Topics 23:1, 213-36.

2004. "Closure Matters: Skepticism and Easy Knowledge," Philosophical Issues 14, 165–84.

2007. "Human Knowledge and the Infinite Progress of Reasoning," Philosophical Studies 134:1, 1–17.

2008. "Useful False Beliefs," in Q. Smith, ed. Epistemology: New Essays (Oxford University Press), 25-61.

Kratzer, A. 1977. "What 'Must' and 'Can' Must and Can Mean," Linguistics and Philosophy 1:3, 337-55.

Kripke, S. 1982. Wittgenstein on Rules and Private Language (Cambridge, MA:

Harvard University Press).
2011. "Nozick on Knowledge," in *Philosophical Troubles: Collected Papers*, vol. 1 (New York: Oxford University Press), 162-224.

Kvanvig, J. L. 2003. The Value of Knowledge and the Pursuit of Understanding (Cambridge University Press).

2004. "Nozickian Epistemology and the Value of Knowledge," Philosophical Issues 14:1, 201-18.

2006. "Closure Principles," Philosophy Compass 1:3, 256-67.
2008. "Closure and Alternative Possibilities," in Greco, J., editor, Oxford Handbook of Skepticism, pages 456-484 (Oxford University Press).

2009a. "Precis of the The Value of Knowledge and the Pursuit of Understanding," in D. H. Pritchard, H. and A. Millar, eds. Epistemic Value (Oxford University Press), 309-11.

Value, pages 339-353. (Oxford University Press). 2009c. "The Value of Understanding," in Pritchard, H. and Millar, editors. 2009b. "Responses to Critics," in Pritchard, H. and Millar, editors, Epistemic

Epistemic Value, pages 95-112 (Oxford University Press).

2010. "The Swamping Problem Redux: Pith and Gist," in A. Haddock, A. Millar, and D. H. Pritchard, eds. Social Epistemology (Oxford University Press), 89-112.

2011. Destiny and Decision: Essays in Philosophical Theology (Oxford University

Understanding," in T. Henning and D. Schweikard, eds. Knowledge, Virtue, and Action (Abingdon: Routledge). "Curiosity and a Response-Dependent Account of the Value of

Lackey, J. 2008. "What Luck Is Not," Australasian Journal of Philosophy 86:2.

Lange, M. 2009. Laws and Lawmakers (Oxford University Press) 2009. "Knowledge and Credit," Philosophical Studies 142:11, 27-42.

Lehrer, K. 1974. Knowledge (Oxford University Press)

Lehrer, K. and Paxson, T. 1969. "Knowledge: Undefeated Justified True Belief," Journal of Philosophy, 66:8, 225-37.

Levy N. 2009. "What, and Where, Luck Is: A Response to Jennifer Lackey," Australasian Journal of Philosophy 87:3, 489–97.

Lewis, D. 1973. Counterfactuals (Oxford: Blackwell Publishing).

1977. "Possible-World Semantics for Counterfactual Logics: A Rejoinder," Journal of Philosophical Logic 6:1, 359–63.

1979. "Counterfactual Dependence and Time's Arrow," Noûs 13:4, 455-76. 1980. "Veridical Hallucination and Prosthetic Vision," Australasian Journal of

Philosophy 58:3, 239-49.

1996. "Elusive Knowledge," Australasian Journal of Philosophy 74:4, 549–67. 1997. "Finkish Dispositions," Philosophical Quarterly 47:187, 143–58. Lipson, M. 1987. "Nozick and the Sceptic," Australasian Journal of Philosophy

65:3, 327-34.
Lipton, P. 1990. "Contrastive Explanations," in D. Knowles, ed. Explanation and Its Limits (Cambridge University Press), 247-66.

Luper, S. 2003. "Indiscernability Skepticism," in S. Luper, ed. The Skeptics. Ashgate), 183-202. Contemporary Essays, Ashgate Epistemology and Mind Series (Aldershot:

Luper-Foy, S. [now "Luper"] 1984. "The Epistemic Predicament: Knowledge, Nozickian Tracking, and Scepticism," Australasian Journal of Philosophy 62:1, 26-49.

1987a. "Introduction," in S. Luper-Foy, ed. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ: Rowman & Littlefield), 1-16.

1987b. "The Possibility of Skepticism," in S. Luper-Foy, ed. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ: Rowman & Littlefield),

Luper-Foy, S., ed. 1987c. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ: Rowman & Littlefield)

Madison, B. J. C. 2011. "Combating Anti-Anti-Luck Epistemology," Australasian Journal of Philosophy 89:1, 47–58.

Manley, D. 2007. "Safety, Content, Apriority, Self-Knowledge," Journal of Philosophy 104:8, 403-23.

Manley, D. and Wasserman, R. 2008. "On Linking Dispositions and Conditionals," Mind 117:465, 59-84.

Martin, C. B. 1994. "Dispositions and Conditionals," Philosophical Quarterly 44:174, I-8.

2007. The Mind in Nature (Oxford University Press).

Mazoué, J. G. 1986. "Some Remarks on Luper-Foy's Criticism of Nozickian Tracking," Australasian Journal of Philosophy 64:2, 206-12.

Knowledge," Journal of Philosophical Research 34, 10–20. McGinn, C. 1984. "The Concept of Knowledge," Midwest Studies in Philosophy McEvoy, M. 2009. "The Lottery Puzzle and Pritchard's Safety Analysis of

9, 529-54.

McKinsey, M. 1991. "Anti-Individualism and Privileged Access," Analysis 51:1,

Molnar, G. 2003. *Powers: A Study of Metaphysics* (Oxford University Press). Murphy, P. 2005. "Closure Failures for Safety," *Philosophia* 33, 331–34. Neta, R. and Rohrbaugh, G. 2004. "Luminosity and the Safety of Knowledge," Pacific Philosophical Quarterly 85, 396–406.

Nozick, R. 1981. Philosophical Explanations (Cambridge, MA: Harvard University Press).

Olsson, E. and Goldman, Alvin. 2009. "Reliabilism and the Value of Knowledge," in A. Haddock, A. Millar, and D. H. Pritchard, eds. *Epistemic* Value (Oxford University Press), 19-41.

Pritchard, D. H. 2002. "Resurrecting the Moorean Response to the Sceptic," International Journal of Philosophical Studies 10, 283–307.

2004. "Epistemic Luck," Journal of Philosophical Research 29, 193–222 2005a. Epistemic Luck (Oxford University Press).

2005b. "Scepticism, Epistemic Luck and Epistemic Angst," Australasian Journal of Philosophy 83:2, 185-206.

2007a. "Anti-Luck Épistemology," Synthese 158:3, 277-97.
2007b. "Knowledge, Luck, and Lotteries," in V. F. Hendricks and D. H. Pritchard, eds. New Waves in Epistemology (Basingstoke: Palgrave Macmillan), 28-51.

2007c. "The Value of Knowledge," in E. Zalta, ed., Stanford Encyclopedia of value/. Last accessed June 2011. Philosophy. http://plato.stanford.edu/archives/fall2007/entries/knowledge-

2008a. "Radical Scepticism, Epistemic Luck and Epistemic Value," Proceedings and Addresses of the Aristotelian Society (suppl. vol.) 82, 19–41.

2008b. "Sensitivity, Safety, and Anti-Luck Epistemology," in J. Greco, ed. The

Oxford Handbook of Skepticism (Oxford University Press), 437–55. 2009a. "Apt Performance and Epistemic Value," Philosophical Studies 143:3,

2009b. "Safety-Based Epistemology: Whither Now?" Journal of Philosophical 407-16.

Research 34, 33-45. in press-a. "Anti-Luck Virtue Epistemology," Journal of Philosophy.

in press-b. "There Cannot Be Lucky Knowledge," in M. Steup and J. Turri, Publishing). eds. Contemporary Debates in Epistemology, 2nd edn. (Oxford: Blackwell

Pritchard, D. H., Millar, A., and Haddock, A. 2010. The Nature and Value of Knowledge: Three Investigations (Oxford University Press).

Pritchard, D. H., and Smith, M. 2004. "The Psychology and Philosophy of Luck," New Ideas in Psychology 22, 1-28.

Putnam, H. 1981. Reason, Truth and History (Cambridge University Press)

Quine, W. 1969. "Epistemology Naturalized," in Ontological Relativity and Other Essays (New York: Columbia University Press), 69–90.

Riggs, W. 2007. "Why Epistemologists Are So Down on Their Luck," Synthese

158:3, 329–44.
2009. "Luck, Knowledge and Control," in A. Haddock, A. Millar, and D. H. Pritchard, eds. *Epistemic Value* (Oxford University Press), 204–21.

Pritchard, eds. "Expression of Control of Semantic Pritchard, eds." Journal of Semantic

van Rooij, R. 2006. "Free Choice Counterfactual Donkeys," Journal of Semantics 23:4, 383-402.

2010. "Conjunctive Interpretation of Disjunctions," Semantics and Pragmatics 3:II, I—28.

Roush, S. 2005. Tracking Truth: Knowledge, Evidence, and Science (Oxford University Press).

2009. "Précis of Tracking Truth," and "Replies to Critics," Philosophy and Phenomenological Research 79:1, 213–22; 240–47.

2010a. "The Value of Knowledge and the Pursuit of Survival," Metaphilosophy 41:3, 255-78.

2010b. "Closure on Skepticism," *Journal of Philosophy* 107:5, 243–56. in press. "Skepticism about Reasoning," in G. Restall and G. Russell, eds. *New* Waves in Philosophical Logic (Basingstoke: Palgrave Macmillan),

Russell, B. 1948. Human Knowledge: Its Scope and Limits (New York: Simon & Schuster).

Sainsbury, R. M. 1997. "Easy Possibilities," Philosophy and Phenomenological

Research 57:4, 907–19.
Schulz, K. 2005. "Minimal Models in Semantics and Pragmatics: Free Choice, Exhaustivity, and Conditionals" (doctoral dissertation, Universiteit van Amsterdam).

Littlefield), 242–66. Shope, R. 1978. "The Conditional Fallacy in Contemporary Philosophy," Journal Shatz, D. 1987. "Nozick's Conception of Skepticism," in S. Luper-Foy, ed. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ: Rowman &

of Philosophy 75:8, 397-413.

1983. The Analysis of Knowing: A Decade of Research (Princeton, New Jersey: Princeton University Press)

1984. "Cognitive Abilities, Conditionals, and Knowledge: A Response to Nozick," *Journal of Philosophy* 81:1, 29–48.

64:12, 373-89.
Smith, A. D. 1977. "Dispositional Properties," Mind 86:343, 439-45. Skyrms, B. 1967. "The Explication of 'X Knows That p'," Journal of Philosophy,

Sosa, E. 1999a. "How Must Knowledge Be Modally Related to What Is Known?" Philosophical Topics 26:1/2, 373-84.

1999b. "How to Defeat Opposition to Moore," Philosophical Perspectives 13,

2000. "Skepticism and Contextualism," Philosophical Issues 10:1, 1–18.

2002. "Tracking, Competence, and Knowledge," in P. Moser, ed. *The Oxford Handbook of Epistemology* (New York: Oxford University Press), 264–86.

2003. "Neither Contextualism nor Skepticism," in S. Luper, ed. The Skeptic: Ashgate), 165–82. Contemporary Essays, Ashgate Epistemology and Mind Series (Aldershot:

> 2004. "Replies," in J. Greco, ed. Sosa and His Critics (Oxford: Blackwell Publishing), 275–326.

2007. A Virtue Epistemology. Apt Belief and Reflective Knowledge, vol. 1 (Oxford University Press).

2009. Reflective Knowledge. Apt Belief and Reflective Knowledge, vol. 11 (Oxford University Press).

Logical Theory (Oxford: Blackwell Publishing), 98–112.
Steinberg, J. 2010. "Dispositions and Subjunctives," Philosophical Studies 148:3, Stalnaker, R. 1968. "A Theory of Conditionals," in N. Rescher, ed. Studies in

Sturgeon, S. 1993. "The Gettier Problem," Analysis, 53:156–64.
Thompson, A. 1986/87. "Counterexamples to Nozick's Account of Transmission of Knowledge via Proof," Philosophy Research Archive 12, 261–65.

Unger, P. 1968. "An Analysis of Factual Knowledge," Journal of Philosophy 65:6. 157–70.

1975. Ignorance: A Case for Skepticism (Oxford University Press).
Vogel, J. 1987. "Tracking, Closure, and Inductive Knowledge," in S. Luper-Rowman & Littlefield), 197-215. Foy, ed. The Possibility of Knowledge: Nozick and His Critics (Totowa, NJ:

Kluwer), 13–27.
1999. "The New Relevant Alternatives Theory," Philosophical Perspectives 13, 1990. "Are There Counterexamples to the Closure Principle?" in M. D. Roth and G. Ross, eds. Doubting: Contemporary Perspectives on Skepticism (Dordrecht

155–80.

2000. "Reliabilism Leveled," Journal of Philosophy 97:11, 602–23, 2004. "Skeptical Arguments," Philosophical Issues 14:1, 426–55.

2007. "Subjunctivitis," *Philosophical Studies* 134:1, 73–88. Williams, J. R. G. 2008. "Chances, Counterfactuals, and Similarity," *Philosophy*

Williams, M. 1996. Unnatural Doubts: Epistemological Realism and the Basis of and Phenomenological Research 77:2, 385-420.

2002. "Nozick on Knowledge and Skepticism," in D. Schmidtz, ed. Robert Scepticism (Princeton University Press).

Nozick (Cambridge University Press), 131-54.

Williamson, T. 2000. Knowledge and Its Limits (Oxford University Press).
Wright, C. 1985. "Facts and Certainty," Proceedings of the British Academy 71, 429-72.

2000. "Cogency and Question-Begging: Some Reflections on McKinsey's Paradox and Putnam's Proof," *Philosophical Perspectives* 10 (Skepticism), 140-63.

2003. "Some Reflections on the Acquisition of Warrant by Inference," in S. Nuccetelli, ed. New Essays on Semantic Externalism, Scepticism, and Self-Knowledge (Cambridge, MA: MIT Press), 57-77.

Zagzebski, L. 1994. "The Inescapability of the Gettier Problem," Philosophical Quarterly, 44:174, 65-73.